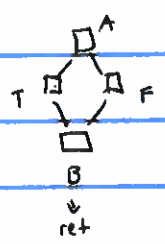


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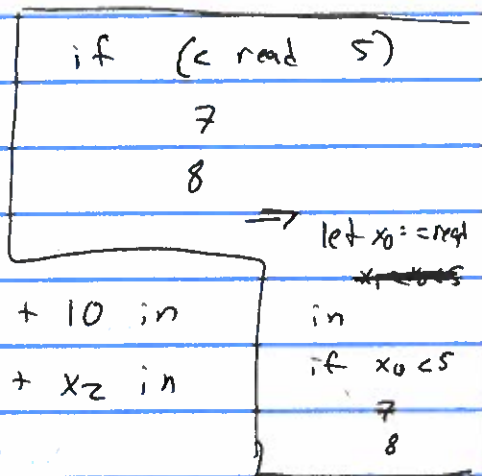
rco removes the "recursive" structure from R

$R_2$   $(+ (if (< (read) 5) 17 (+ 8 (+ 9 10))))$   
 $(+ (read) 21)$

$R_{CO_2}$  let  $x_0 := read$  in  
 let  $x_1 := if$   $x_0 < 5$



then 17  
 else let  $x_2 := 9 + 10$  in  
 let  $x_3 := 8 + x_2$  in  
 $x_3$



in  
 let  $x_4 := read$  in  
 let  $x_5 := x_4 + 21$  in  
 $x_5$

let\* : List (Pair Var Expr)  
 \* Expr  
 → Expr

$rco_p : R_{progs} \Rightarrow R_{progs}$

$rco_p$  (program i e) = (program i (rcoe  $\emptyset$  T e))

$rcoe : (X \Rightarrow E) TailPos? e \Rightarrow e$

$rcoe \sigma tail? e := let^* nv e1$

where (nv, e1) =  $rcoa \sigma tail? e$

$rcoa : (X \Rightarrow E) TailPos? e \Rightarrow (List (Pair Var E)) \times E (arg)$

$rcoa \sigma tail? (var x) := (mt, \sigma(x))$

$rcoa \sigma tail? \binom{num\ n}{pool\ b} := (mt, \binom{num\ n}{pool\ b})$

(read) := ([ (read-var, read) ], read-var)

(una a) := (nva ++ [(unavar, (una a'))], unavar)

where (nva, a') =  $rcoa \sigma F a$

8-2/  $\text{rcoa } \sigma \text{ tail? (bin } e_L \text{ } e_R) :=$

$(\text{nv}_L ++ \text{nv}_R ++ [(\text{binvar}, (\text{bin } a_L \text{ } a_R))], \text{binvar})$

where  $(\text{nv}_L, a_L) = \text{rcoa } \sigma \text{ F } e_L$

$(\text{nv}_R, a_R) = \text{rcoa } \sigma \text{ F } e_R$

$\text{rcoa } \sigma \text{ tail? (let } x := x_e \text{ in } b_e) :=$

$(\text{nv}_x ++ \text{nv}_b, a_b)$

where  $(\text{nv}_x, a_x) := \text{rcoa } \sigma \text{ F } x_e$

$\sigma' := \sigma [x \mapsto a_x]$

$(\text{nv}_b, a_b) := \text{rcoa } \sigma' \text{ tail? } b_e$

$\text{rcoa } \sigma \text{ tail? (if } e_c \text{ } e_T \text{ } e_F) :=$

$\boxed{\text{if}}$  tail?  $\boxed{\text{then}}$

$(\text{nv}_c, \text{if}')$

$\boxed{\text{else}}$   $(\text{nv}_c ++ [(\text{ifvar}, \text{if}')], \text{ifvar})$

where  $(\text{nv}_c, \text{cmp}_c, a_L, a_R) :=$

$\text{rco}_c \sigma \text{ } e_c$

$\text{if}' := \text{if } (\text{cmp}_c \text{ } a_L \text{ } a_R)$

then  $\text{rco}_e \sigma \text{ tail? } e_T$

else  $\text{rco}_e \sigma \text{ tail? } e_F$

$\text{rco}_c : (X \rightarrow E) \ E \Rightarrow (\text{newvars}, \text{cmp op}, A, A)$

$\text{rco}_c \sigma \text{ (bin op } e_L \text{ } e_R) :=$

$(\text{nv}_L ++ \text{nv}_R, \text{op}, a_L, a_R)$

where  $(\text{nv}_L, a_L) = \text{rco}_a \sigma \text{ F } e_L$

$(\text{nv}_R, a_R) = \text{rco}_a \sigma \text{ F } e_R$

$\text{rco}_c \sigma \text{ (let } x := x_e \text{ in } b_e) :=$

$(\text{nv}_x ++ \text{nv}_b, \text{op}_b, a_L, a_R)$

where  $(\text{nv}_x, a_x) = \text{rco}_a \sigma \text{ F } x_e$

$(\text{nv}_b, \text{op}_b, a_L, a_R) = \text{rco}_c \sigma' \text{ } b_e$

$\sigma' = \sigma [x \mapsto a_x]$

$\text{rco}_c \sigma \text{ other} := (\text{nv}, \overset{\text{bool}}{=}, T, a)$

where  $(\text{nv}, a) = \text{rco}_a \sigma \text{ F other}$

$$\text{ecomp} : \mathcal{R} \Rightarrow \mathcal{C}$$

if (= 5 6)      goto-if (= 5 6)    Block1    Block2  
 12  
 or let x := ...      Block2 = seq (set x = ...)    ...

$$\text{ecomp} (\text{program} ; \text{be}) = (\text{program} ; L \Rightarrow T [\text{BODY} \mapsto t_b])$$

where  $(L \Rightarrow T, t_b) = \text{econe } \text{be} (\lambda (fa) (\text{return } fa))$

$$\text{econe } k \text{ boring } (\text{var}, \text{num}, \text{bool}) = (\emptyset, k (\text{econa boring}))$$

$$\text{econe } k (\text{let } x := x_e \text{ in } \text{be}) = (L \Rightarrow T, (\text{seq } (\text{set! } x (\text{econe } x_e)) \text{ b}^+))$$

where  $(L \Rightarrow T, \text{b}^+) = \text{econe } k \text{ be}$

$$\text{econe } k (\text{if } (\text{cmp } a_L \ a_R) \ e_T \ e_F) = (L \Rightarrow T_T \ ++ \ L \Rightarrow T_F \ ++ \ \text{NEW},$$

where  $(L \Rightarrow T_T, T_T) = \text{econe } k \ e_T$       goto-if (cmp a\_L' a\_R')

$(L \Rightarrow T_F, T_F) = \text{econe } k \ e_F$       true-lab

$a_L' = \text{econa } a_L$       false-lab

$a_R' = \text{econa } a_R$

$\text{NEW} = [\text{true-lab} \mapsto T_T, \text{false-lab} \mapsto T_F]$

$$\text{econe } k (\text{let } x := (\text{if } (\text{cmp } a_L \ a_R) \ e_T \ e_F) \ \text{in } \ e_B) =$$

$(L \Rightarrow T_T \ ++ \ L \Rightarrow T_F \ ++ \ L \Rightarrow T_B \ ++ \ \text{NEW},$

goto-if (cmp a\_L' a\_R') true-lab false-lab)

$\text{NEW} = [\text{true-lab} \mapsto T_T, \text{false-lab} \mapsto T_F, \text{suffix-lab} \mapsto T_B]$

$(L \Rightarrow T_T, T_T) = \text{econe } k \ e_T$

$(L \Rightarrow T_F, T_F) = \text{econe } k \ e_F$

$(L \Rightarrow T_B, T_B) = \text{econe } k \ e_B$

$\text{NEW} = (\lambda (fa) (\text{seq } (\text{set! } x \text{ fa}) (\text{goto } \text{suffix-lab})))$

