

7-1/

randp : x Num \rightarrow e
setvars \rightarrow
depth

randp V 0 = number
variable-reference (if vars)
bool (50% true / 50% false)
(+ 1 true)

randp : (~~Type~~) (Type \rightarrow set(vars))
x Type (T)
x Num (depth)
 \rightarrow expression of type T

randp N = rande (M+) (Random (Int or Bool)) N

rande Σ Bool 0 = true / false / vars (Σ (Bool))
Num 0 = num / vars (Σ (Num))

Bool (1+n) = \oplus (cmp (rande Σ Num n)
 $\xrightarrow{T_1}$ random (rande Σ Num n))

VS' = Σ (T) \cup {x}
 Σ' = Σ [T \rightarrow VS']
② let x := xe in b T
where xe := rande Σ (~~Bool~~) N
b := rande Σ (T) [add x] Bool

Σ'' = remove x from the other types
③ (if (rande Σ Bool N) T_1 N
(rande Σ T₁ N) (rande Σ T₂ N))

7-2) What optimization apply to RZ?

booleans are "simple"

(cmp N_1, N_2) can reduce to a value

(if B, e_T, e_F) = either e_T or e_F depending on B ,

(not (not e)) $\rightarrow e$

(not x) = (if x f t)

(if (if e f t) f t) $\rightarrow e$

(if (not c) t f) \rightarrow (if c f t)

purity

~~if~~ ($= e_1, e_1$) \rightarrow true if e_1 "has no read"

opt : ($v \rightarrow e$) \times $e \rightarrow e$

change! $e \times$ bool \times set(vars)

($< e_1, (+ N e_1)$) \rightarrow true if $N > 0$

\rightarrow used vars

(if c, e_1, e_2) \rightarrow seq (c, e_1)

$c' = X^{e_1} + e_2$:=

if $c' = x$, then opt $\{ [x \rightarrow true]$
 et
 opt $\{ [x \rightarrow false]$
 et

seq : $e \times e \rightarrow e$

\rightarrow returns this value after this effect

seq ($+ N$ read) $\perp Z =$ (let $- :=$ read in $\perp Z$)

seq true $\perp Z = \perp Z$

opt Σ (let $x := x_e$ in b) = ($x_e', x_e\text{-pure?}, x_e\text{-vars}$) = opt Σ x_e
 if x & $b\text{-vars}$ $\Sigma' = \Sigma [x \rightarrow x_e' \text{ if pure a.w. } x]$

(seq $x_e' b'$), (and $x_e\text{-pure?}$, $\cup x_e\text{-vars}$) (b', b-pure?, b-vars) = ^{are simple} opt $\Sigma' b$

a.w.

(let $x := x_e'$ in b'), $x_e\text{-vars} \cup (b\text{-vars} - \Sigma x)$

7-3

$C_0 \rightarrow C_1$

$C_1 :=$ arg := ... | true | false

cmp := ... | < | ≤ | > | >

exp := ... | (not arg) | (cmp arg arg)

tail := ... | (goto label) | (goto-if (cmp a u) label label)

interp_c : (label → tail) tail

L+T (goto label) = interp_c L+T L+T(label)

X_0 to X_1

$X_1 :=$ arg := ... | byte-reg register (byte-reg rax)

cc := e | l | le | g | ge ⇒ %a1

instr := ... | xorq a, a | cmpq a, a |

| set_cc a | movzbg a, a | jmp-if cc label
no space in printing prints jmpcc label

remember `cmpq $4, $5` $5 < 4$

`set l, %eax` ⇒ FALSE

both `cmpq` and `movzbg` cannot have nums in 2nd position

rc0 updated for R_z

$rc0-e :=$... | (if (cmp rc0-a rc0-a) rc0-e rc0-e)

$rc0-c :=$... | (not rc0-a) | (cmp rc0-a rc0-a) |
| (if (cmp rc0-a rc0-a) rc0-e rc0-e)

$rc0-a :=$... | bools (+ & f)

7-4/

$\rho(\sigma \text{ (if } e_c \ e_+ \ e_f) :=$

$(nv_c, a_c) := \rho(\sigma \ e_c$ ~~$\rho(\sigma \ e_c$~~

$(nv_+, a_+) := \rho(\sigma \ e_+ \quad (nv_c \ ++ \ nv_+ \ ++ \ nv_f \ ++ \ (x, if$

$(nv_f, a_f) := \rho(\sigma \ e_f$

$if \ (cmp \ a_L \ a_R)$