

7-1

$R_e = \dots | (\text{if } e_1 e_2 e_3) | \#+ | \#f$
 $| (\text{and } e_1 e_2) | (\text{or } e_1 e_2) | (\text{not } e)$
 $| (\text{cmp } e_1 e_2)$

$\text{cmp} = \text{eq} | \text{lt} | \text{gt} | \dots$

$$E[(\text{if } \#+ e_1 e_2)] \Rightarrow E[e_1] \\ \#f \qquad \qquad \qquad \Rightarrow e_2$$

$E = \dots | (\text{and } E e) | (\text{and } \vee E)$

$$(+ \#+ 3) \Rightarrow \perp \\ (+ \times 3)$$

$T = \text{Int} | \text{Bool} |$

$\text{Ty}(: R \rightarrow T \text{ (or crash)}) \quad (\text{put before/after unicity})$

$\text{Ty}(: \text{env}(\text{var} \rightarrow T) \quad R \rightarrow T$

$T(\Gamma, \text{int}) = \text{Int}$

$T(\Gamma, \#+) = \text{Bool}$

$T(\Gamma, (+ e_1 e_2)) = \text{if } T(\Gamma, e_1) = \text{Int} \text{ or } T(\Gamma, e_2) = \text{Int},$
 then Int or error

$T(\Gamma, (\text{cmp } e_1 e_2)) = T(\Gamma, e_1) = \text{Int} \wedge T(\Gamma, e_2) = \text{Int} \wedge \text{Bool}$

$T(\Gamma, \times) = \Gamma(x)$

$T(\Gamma, \text{let}(x, x_e, b_e)) =$

$T(\Gamma[x \mapsto T(\Gamma, x_e)], b_e)$

$T(\Gamma, (\text{if } e_c e_t e_f)) =$

$T(\Gamma, e_c) = \text{Bool}$

$T(\Gamma, e_t) = T(\Gamma, e_f)$

$T(\Gamma, e_t)$

7-2/

flatten : $R^+_p \rightarrow C.p$

$C.p = (\text{program } e)$

$C.p = (\text{program vs ss } a +)$

$C.p = (\text{program vs ss } a)$

$C.a = \text{int } | \text{ var}$

$R^+_p = (\text{program } + e)$

$C.e = (\text{read}) | (+ a a) | (- a) | (\text{and}) | (\text{or}) | (\text{cmp } (\text{not})$

$C.s = (\text{set! } x e) | (\text{if } (\text{cmp } a a) \vec{s} \vec{s}) [\text{hard}]$

$(\text{if } a \vec{s} \vec{s}) [\text{easy}]$

$(\text{eg } 1 a)$

easy: flatten(if(ec, e+, ef))

$\langle vsc, ssc, ac \rangle = \text{flatten}(ec)$

$\langle vs+, ss+, at \rangle = \text{flatten}(e+)$

$\langle vsf, ssf, af \rangle = \text{flatten}(ef)$

let vif be a new variable

$\langle vif \# vsc \# vs+ \# vsf, ssc ++ (\text{if } (\text{eq } 1 ac) \cancel{\# vif}, ss+ ++ (\text{set! } vif a+), ssf ++ (\text{set! } vif af)) \rangle,$

$vif \rangle$

hand:

flatten^{HC} : $R^+_p, e \rightarrow C.p^{HC}$

$C.p^{HC} = (\text{program vs}$

$fHC(\text{Int}) = \langle \dots, 1 \rangle$

ss

$fHC(\#) = \langle \dots, \text{eq } 1 1 \rangle$

a

$fHC(\#f) = \langle \dots, \text{eq } 1 0 \rangle$

$\text{Maybe } (\text{cmp } a a))$

$fHC(\text{eg } e_1 e_2) = \langle \dots, \text{eg } e_1 e_2 \rangle$

$\forall s = \text{Veg} ++ vs, ++ vs_2$

$ss = ss_1 ++ ss_2 ++ (\text{set! } \text{Veg } (\text{eq } a_1 a_2))$