

19-V

$I (assign x e) r p k \sigma =$

$\text{if } p(x) = \text{Var}(x', \text{op}, s, l_x)$

$\text{if ref } \notin s, \text{ then}$

$I e \text{ Effect } r p k \sigma$

O.w.

$I e \text{ Value } r p k, \sigma$

$k, e' \sigma_1 = k (\text{seq assign } x' e') (\text{const } c) \sigma_2$

$c = \text{true if } r = \text{Test} \text{ o.w. } c = \text{void}$

$\sigma_2 = \sigma_1 [l_{x'} \mapsto \{\text{assign}\} \cup \sigma_1(l_{x'})]$

$I (call e_1 e_2) r p k \sigma =$

$I e_1 r_1 p k_1 \sigma_1$

$r_1 = \text{App}(\text{op}, r, l_{r_1})$

$\text{op} = \text{Opnd}(e_2, p, l_{e_2})$

$\sigma_1 = \sigma [l_{e_2} \mapsto \text{unvisited}, l_{r_1} \mapsto \emptyset]$

$k, e'_1 \sigma_2 = \text{if } \sigma_2(l_{r_1}) \text{ defined then}$

$k e'_1 \sigma_2$

O.w.  $\text{visit}(\text{op}, \text{Value}, k_2, \sigma_2)$

$k_2 e'_2 \sigma_3 = k (\text{call } e'_1 e'_2) \sigma_3$

$\text{visit}(\text{Opnd}(e, p, l_e), r, k, \sigma) =$

$\text{if } \sigma(l_e) = \text{unvisited then } I e r p k, \sigma$

$k, e' \sigma' = k e' \sigma [l_e \mapsto e']$

O.w.  $k \sigma(l_e) \sigma$

19-2)

$I \ (\text{primref } p) \ r \ p \ k \ \sigma =$

if  $r = \text{Test}$  then  $k \ (\text{const true}) \ \sigma$

if  $r = \text{Effect}$  then  $k \ (\text{const void}) \ \sigma$

if  $r = \text{Value}$  then  $k \ (\text{primref } p) \ \sigma$

if  $r = \text{App}(\text{op}, r_1, l_r)$  then  $\text{fold } (\text{primref } p) \ r \ p \ k$

$\text{fold } (\text{primref } p) \ \text{App}(\text{op}, r_1, l_r) \ p \ k \ \sigma =$

$\text{visit}(\text{op}, \text{Value}, k_1, \sigma)$

$k_1 \ e'_1 \ \sigma_1 = \text{if result}(e'_1) = (\text{const } c) \text{ and } \boxed{p(c) = c'}$   
 $k \ (\text{const } c') \ \sigma_2$

$\sigma_2 = \sigma_1 [l_r \mapsto \{\text{inlined}\} \cup \sigma_1(l_r)]$

O.w.  $k \ (\text{primref } p) \ \sigma_1$

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$I \ (\lambda x. e) \ r \ p \ k \ \sigma =$

if  $r = \text{Test}$ ,  $k \ (\text{const true}) \ \sigma$

if  $r = \text{Effect}$ ,  $k \ (\text{const void}) \ \sigma$

if  $r = \text{App}(\text{op}, r_1, l_r)$ ,  $\text{fold } (\lambda x. e) \ r \ p \ k \ \sigma$

if  $r = \text{Value}$ ,  $I \ e \ \text{Value} \ p_1 \ k_1 \ \sigma_1$

$x'$  and  $l_{x'}$  are fresh

$\hat{x}' = \text{Var}(x', \text{null}, \sigma(l_x), l_{x'})$

$p_1 = p [x \mapsto \hat{x}']$

$\sigma_1 = \sigma [l_{x'} \mapsto \emptyset]$

$k_1 \ e' \ \sigma_2 = k \ (\lambda x' \ e') \ \sigma_2$

19-3/ fold (lambda x e). App(op, r<sub>1</sub>, l<sub>r</sub>) p k σ =  
I e r<sub>1</sub> p<sub>1</sub> k<sub>1</sub> σ<sub>1</sub>

$$\hat{x} = \text{Var}(x, \text{null}, s, l_x) \quad x' \text{ and } l_{x'} \text{ are fresh}$$

$$\hat{x}' = \text{Var}(x', op, \sigma(l_x), l_{x'})$$

$$p_1 = p[\hat{x} \mapsto \hat{x}']$$

$$\sigma_1 = \sigma[l_{x'} \mapsto \emptyset]$$

$$k_1 e' \sigma_2 = \text{if ref} \notin \sigma_2(l_{x'}) \text{ and assign} \notin \sigma_2(l_{x'})$$

visit(op, Effect, k<sub>2</sub>, σ<sub>2</sub>)

if ref ∈ σ<sub>2</sub>(l<sub>x'</sub>) and assign ∈ σ<sub>2</sub>(l<sub>x'</sub>)

visit(op, Effect, k<sub>3</sub>, σ<sub>2</sub>)

O.w. visit(op, Value, k<sub>3</sub>, σ<sub>2</sub>)

$$k_2 e' \sigma_3 = K (\text{seq } e' e') \underbrace{\sigma_3[l_r \mapsto \{\text{null}\} \cup \sigma_3(l_r)]}_{\sigma_3(l_r)}$$

$$k_3 e' \sigma_3 = k (\text{call } (\lambda x' e') e') \quad \text{del "}$$

I (ref x) r p k σ =

if r = Effect, K (const void) σ

if p(x) = Var(x', op, s, l<sub>x'</sub>)

and op = null OR assign ∈ s then K (ref x') σ,

$$\sigma_1 = \sigma[l_{x'} \mapsto \{\text{ref}\} \cup \sigma(l_{x'})]$$

O.w. // op isn't null (so we know what we are)

visit(op, Value, k<sub>1</sub>, σ)

$$k_1 e \sigma_2 = \text{copy}(p(x), \text{result}(e), r, k, \sigma_2)$$

9-4/

copy( Var(x', op, s, l<sub>x'</sub>), e, r, k, σ ) =

- 1) if  $e = (\text{const } c)$ ,  $I \not\in r \Rightarrow k \sigma$
- 2) if  $e = (\text{ref } x_i)$  and assign & s,  
 $\hat{x}_i = \text{Var}(x_i / \text{op}_i, s_i, l_{x_i}) / k(\text{ref } x_i) \sigma$
- 3) if  $r = \text{App}(\text{op}_i, r_i, l_r)$   
and  $e = (\text{primref } p)$  or  $e = (\lambda x_i. e_i)$   
then fold  $e - r \not\in k \sigma$
- 4) if  $r = \text{Value}$  and  $e = \text{primref } p$   
 $k(\text{primref } p) \sigma$
- 5) if  $r = \text{Test}$  and  $e = \text{primref, lambda, assign}$   
 $k(\text{const true}) \sigma$
- 6)  $k(\text{ref } x') \sigma_i$  where  $\sigma_i = \sigma[x' \mapsto \text{ref } v \sigma(k)]$