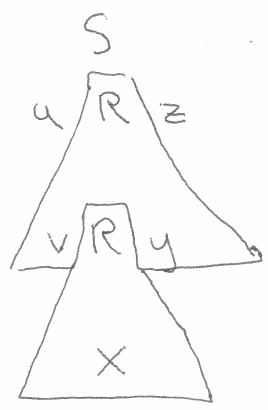




DFA's repeat states on long (accepted) input
CFGs repeat variables

$L(G) = A$
 $\exists (w \mid |w| > 2^{|V|})$
 $\exists G', L(G') \subseteq A$



G'

$S \rightarrow uRz$
 $R \rightarrow vRy$
 $R \rightarrow x$

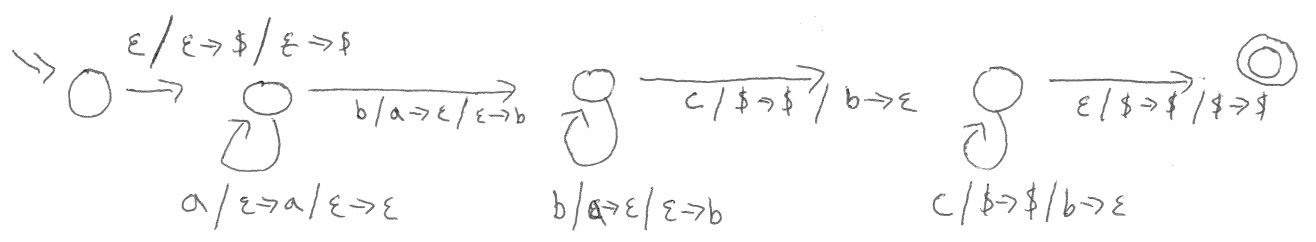
$uv^i xy^i z$ for $i \in \mathbb{N}$

CFPP (Context-free pumping property)

$\forall A \in CFL,$
 $\exists p \in \mathbb{N}, \quad // \quad p = 2^{|V|} + 1$
 $\forall (w \in A \mid |w| \geq p),$
 $\exists (u, v, x, y, z \in \Sigma^* \mid w = uvxyz$
 $\quad \wedge |vy| > 0$
 $\quad \wedge |vxy| \leq p)$
 $\forall i \in \mathbb{N},$
 $uv^i xy^i z \in A$

$a^n b^n c^n \notin CFL$

one change: arbitrary "recall"
 another: 2nd stack



"NFA" = 0-PDA
 "PDA" = 1-PDA
 2-PDA \Rightarrow weird middle ground between CFL and TMs
 3-PDA \Rightarrow TMs

13-2)

$$D = \{ ww \mid w \in \{0,1\}^* \}$$

$$|w| = n \quad \forall k \in \mathbb{N}. \exists (p, l) \text{ s.t. } L(p) = ww \text{ s.t. } (w) \in L(p)$$

$$\exists w. w \in D \wedge w \notin L(p).$$

$$\Rightarrow w = 0^{k+1} 1 0^{k+1}$$

$w w^R$
 $S \rightarrow \epsilon$
 $| 0 S 0$
 $| 1 S 1$

$\forall p \in \mathbb{N}$ (Given p)

$\exists s \in D$ (Choose s)

$$s = 0^p 1 0^p 1$$

$$s = (01)^p (10)^p$$

$$s = 0^p 0^p$$

$$s = 0^p 1^p 0^p 1^p$$

case 1(a-d) vxy mentions 1 symbol
 \Rightarrow clearly fails

case 2(e-g) vxy mentions 2 symbols

L01 and R01 \Rightarrow clearly fail

C10 \Rightarrow can't affect 1st 0s or 2nd 1s

$$E = \{ 0^x \# 0^y \mid x \neq y \}$$

$$S \rightarrow \# \mid 0 S 0 \Rightarrow 0^n \# 0^n$$

$$\begin{array}{l}
 S \rightarrow \# \mid X S X \\
 X \rightarrow X X \mid \epsilon
 \end{array}$$

$$\begin{array}{l}
 S \rightarrow \# \mid 0 X S X \mid X S X 0
 \end{array}$$

$$\begin{array}{l}
 S \rightarrow R \mid 0 S 0 \\
 R \rightarrow X \# \mid \# X \\
 X \rightarrow 0 \mid X
 \end{array}$$

✓ $F = \{ xy \mid x \neq y \text{ but } |x| = |y| \}$

X $G = \{ w \# t \mid t = u w v \text{ for some } u, v \}$