

Control flow analysis

Control Flow Graph Basic Blocks

- Segments of code without transfers of control.

2 techniques

- Continuation Passing Style (CPS)
- Non-standard Abstract Semantics

- all functions get a new argument, κ

All transfers of control are uniform

$(\lambda (v) \dots)$

$(\text{define } (f\ x) \rightarrow (\text{define } (f\ x\ \kappa) \rightarrow$
 $(+ (g\ (h\ x)) (g\ x))) (h\ x\ (\lambda (h\ x)$
 $(+ (g\ h\ x) (g\ x))))))$

$(\text{define } (f\ x\ \kappa)$
 $(h\ x\ (\text{lambda } (h\ x)$
 $(g\ h\ x\ (\text{lambda } (g\ h\ x)$
 $(+ g\ h\ x\ (g\ x)))))))$

\downarrow

$(\text{define } (f\ x\ \kappa)$ $\text{define } (h\ x\ \kappa)$
 $(h\ x\ (\lambda (h\ x)$
 $(g\ h\ x\ (\lambda (g\ h\ x)$
 $(g\ x\ (\lambda (g\ x)$
 $(+ g\ h\ x\ x))))))$

Stop continuation: $(\lambda (v) v)$

NSAS - key behind abstraction is that the accuracy is traded for compile-time computability.

Expr ::= $i \mid (+ e_1 e_2) \mid (* e_1 e_2) \mid (- e)$

$e_1, e_2 \in \text{Expr}$
 $i \in \text{Integer}$

S

$$\llbracket i \rrbracket = i$$

$$\llbracket (+ e_1 e_2) \rrbracket = \llbracket e_1 \rrbracket + \llbracket e_2 \rrbracket$$

$$\llbracket (* e_1 e_2) \rrbracket = \llbracket e_1 \rrbracket * \llbracket e_2 \rrbracket$$

$$\llbracket (- e) \rrbracket = -\llbracket e \rrbracket$$

$$S[\llbracket (+ 2 (* 3 (- 4))) \rrbracket] = 7$$

Non-standard semantics

$$S_{\text{sign}} \llbracket e \rrbracket = \left[\begin{array}{l} - \quad S \llbracket e \rrbracket < 0 \\ 0 \quad S \llbracket e \rrbracket = 0 \\ + \quad S \llbracket e \rrbracket > 0 \end{array} \right]$$

$$S_{\text{sign}} \llbracket (+ 2 (* 3 (- 4))) \rrbracket = -$$

Non-standard Abstract Semantics

\hat{S}_{sign}

$$\hat{S}_{\text{sign}} \llbracket i \rrbracket = S_{\text{sign}} \llbracket i \rrbracket$$

$$\hat{S}_{\text{sign}} \llbracket (+ e_1 e_2) \rrbracket = \hat{S}_{\text{sign}} \llbracket e_2 \rrbracket$$

$\hat{S}_{\text{sign}} \llbracket e_1 \rrbracket$	{-}	{0}	{+}	{-, 0, +}
{-}	{-}	{-}	{-, 0, +}	{-, 0, +}
{0}	{-}	{0}	{+}	{-, 0, +}
{+}	{-, 0, +}	{+}	{+}	{-, 0, +}
{-, 0, +}	{-, 0, +}	{-, 0, +}	{-, 0, +}	{-, 0, +}

$$\hat{S}_{\text{sign}} \llbracket (* e_1 e_2) \rrbracket = \hat{S}_{\text{sign}} \llbracket e_2 \rrbracket$$

$\hat{S}_{\text{sign}} \llbracket e_1 \rrbracket$	{+}	{0}	{-}	{-, 0, +}
{0}	{0}	{0}	{0}	{0}
{+}	{-}	{0}	{+}	{-, 0, +}
{-, 0, +}	{-, 0, +}	{0}	{-, 0, +}	{-, 0, +}

$$\hat{S}_{\text{sign}} \llbracket (+ 2 (* 3 (- 4))) \rrbracket =$$

$$(+ \{+\} (* \{+\} (- \{+\})))$$

$$(+ \{+\} (* \{+\} \{-3\}))$$

$$(+ \{+\} \{-3\})$$

$$\{-, 0, +\}$$

Contours

Variable environment
Contour environment.

Define $(f \times K)$
(zero