

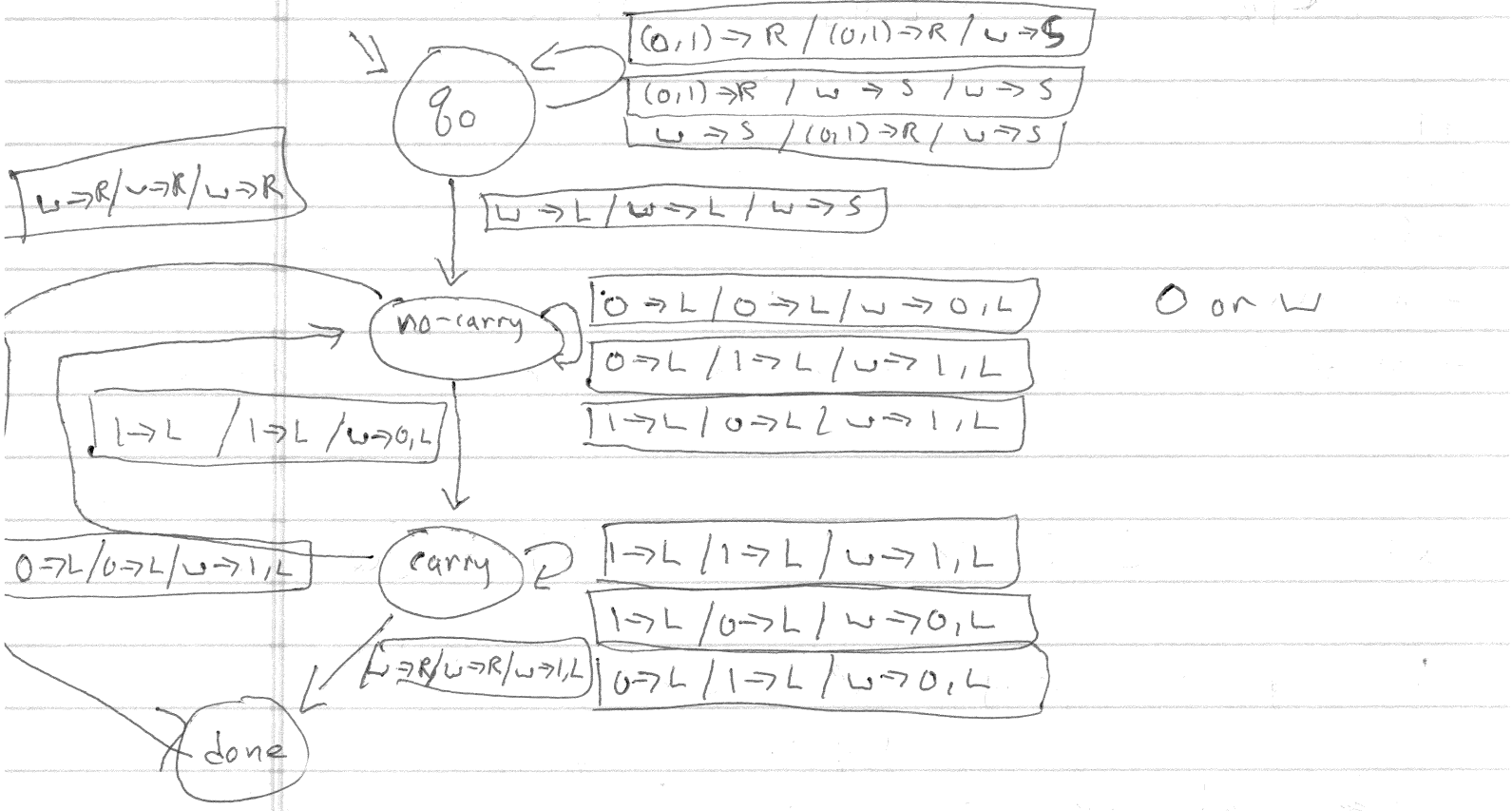
20-1/

3-tape machine (tape 1 = LHS, tape 2 = RHS, tape 3 = 4)

$$\begin{bmatrix} q_0 \\ \\ \epsilon \end{bmatrix} \begin{matrix} 0110 \\ 1010 \\ \end{matrix}$$

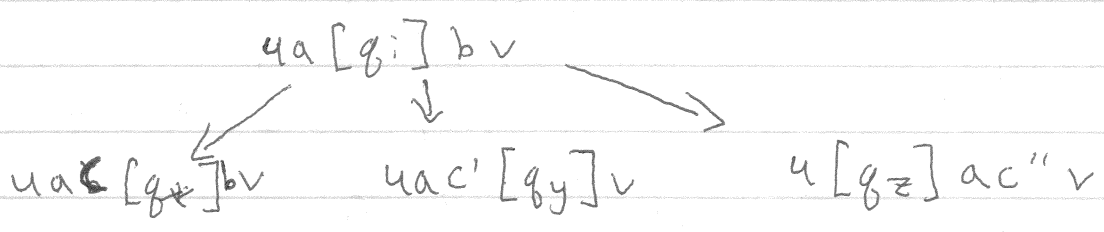
$\Rightarrow^*$

$$\begin{bmatrix} q_{done} \\ \\ 10000 \end{bmatrix} \begin{matrix} 0110 \\ 1010 \\ \end{matrix}$$



# 20-2 / Non-deterministic TM

$$Q \times \Gamma \rightarrow P(Q \times \Gamma \times \{L, R\})$$



## NFA

- ↳ oracle  $\longrightarrow$  can't compile
- ↳ forking  $\longrightarrow$  can compile through fork machine
- ↳ back-tracking
- ↳ set of fringe states  $\longrightarrow$  can't work because of infinite paths

$$\text{Fork-TM} : Q \times \Gamma \rightarrow (Q \times \Gamma \times \{L, R\}) + (Q \times Q)$$

fork-config = set of config  $\delta(q_i, b) = (q_x, q_y)$   $\nearrow$  forked

~~$\{ qa[qi]bv \} \cup S$~~   $\Rightarrow S \cup \{ qa[c][q_i]v \}$

and  $\delta(q_i, b) = (q_i, c, R)$

~~$\{ qa[qi]bv \} \cup S$~~   $\Rightarrow S \cup \{ qa[q_x]bv \}$   
 $\cup \{ qa[q_y]bv \}$

and  $\delta(q_i, b) = (q_x, q_y)$

$$L(\text{fTM}) = \{ w \mid \{ [q_0]w \} \Rightarrow^* S \cup \{ a[q_a]v \} \}$$

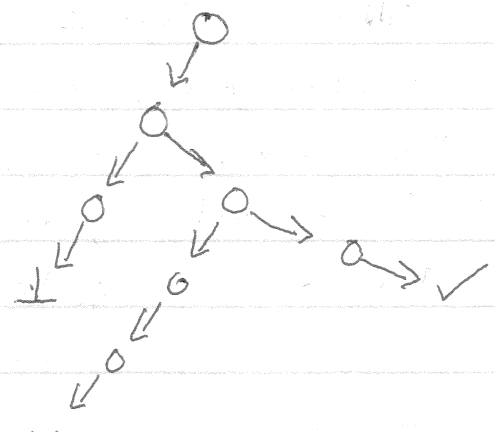
If  $\delta_{nd}(q_i, b) = \{ (q_j, c, L), (q_k, c', R) \}$   
 then  $\delta_F(\hat{q}_i, b) = (\hat{q}_{i1}, \hat{q}_{i2})$   
 $\delta_F(\hat{q}_{i1}, b) = (\hat{q}_j, c, L)$   
 $\delta_F(\hat{q}_{i2}, b) = (\hat{q}_k, c', R)$

Fork  $\Rightarrow$  Normal

$\{ u[q_i]v, x[q_i]y, z[q_k]h \}$

$\Rightarrow$  [start]  $\hat{u}[q_i]v; \hat{x}[q_i]y; \hat{z}[q_k]h$

Back-tracking



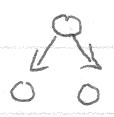
depth-search

(try until failure then go back)

$\Rightarrow$  fails because of divergence

breadth-first

$\delta(q_i, b) = \text{Options} \in [0, 2^{|b| \times |r| \times 2}]$



$|opts|=1$

$|opts|=2$

$|opts|=4$

Some maximum option-size = M

if we have M symbols = 0 ... m = MM

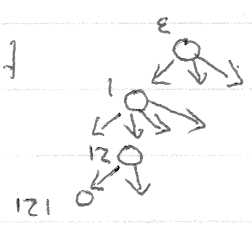
then  $M^*$  = a string of options

$\rightarrow \epsilon$  = no options

address  $\rightarrow$  121 = first, second, first



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(sometimes addresses

don't name configurations)

ordering of addresses:

$\epsilon, 1, 2, 3, 4, 11, 12, 13, 14, 21, 22, 23, 24, \dots$

## 20-4 / 3-tape machine

input = w

tape 1: input  
tape 2: address  
tape 3: simulation

- 1) copy input to tape 3  
with  $[q_0]$  as state  
tape 3 =  $[q_0]w$
- 2) simulate machine based on  
address  $m$  tape 2
- 3) if address ends, fail, but if  
machines accept, then accept
- 4) if we fail, generate next  
address and go to 1

## Enumerator = TM

Have Enum  $\Rightarrow$  Get TM

:

TM (input w)

Run Enum

If it outputs w, accept

Have TM  $\Rightarrow$  Get Enum

:

Enum()

For  $i \in \mathbb{N}$ ,

Run TM on  $s_i$

for only  $i$  steps

(where  $s_i$  is the  
 $i$ th string in

lexicographic order

if accepts, then print  $s_i$