

19-1)

$$I(\text{const } c) \gamma p k \sigma =$$
$$\begin{cases} K(\text{const void}) \sigma & \text{if } \gamma = \text{Effect} \\ K(\text{const true}) \sigma & \text{if } \gamma = \text{Test and } c \neq \text{false} \\ K(\text{const } c) \sigma & \text{o.w.} \end{cases}$$

$$I(\text{seq } e_1, e_2) \gamma p k \sigma =$$

$$\begin{aligned} I e_1 \text{ Effect } p \\ (\lambda e'_1 \sigma'. I e_2 \gamma p \\ (\lambda e'_2 \sigma''. K \text{ seq}(e'_1, e'_2) \sigma'') \sigma') \sigma \end{aligned}$$

$$\begin{aligned} \text{seq}(e_1, e_2) = e_2 & \text{ if } e_1 = (\text{const void}) \\ (\text{seq } (\text{seq } e_1, e_3) e_4) & \text{ if } e_2 = (\text{seq } e_3 e_4) \\ (\text{seq } e_1, e_2) & \text{ o.w.} \end{aligned}$$

$$\begin{aligned} \text{result}(e) = e_2 & \text{ if } e = (\text{seq } e_1, e_2) \\ e & \text{ o.w.} \end{aligned}$$

$$I(\text{if } e_1, e_2, e_3) \gamma p k \sigma =$$

$$I e_1 \text{ Test } p k. \sigma$$

where $K_1 e'_1 \sigma' = \text{if result}(e'_1) = (\text{const true})$

$$I e_2 \gamma_1 p (\lambda e'_2 \sigma'', K \text{ seq}(e'_1, e'_2) \sigma'')$$

$\gamma_1 = \text{Value if } \gamma = \text{App}$ if $\text{result}(e'_1) = (\text{const false})$

γ o.w.

$$I e_3 \gamma_1 p (\lambda e'_3 \sigma''', K \text{ seq}(e'_1, e'_3) \sigma''')$$

o.w.

$$I e_2 \gamma_1 p (\lambda e'_2 \sigma'', I e_3 \gamma_1 p k_2 \sigma'')$$

$$K_2 e'_3 \sigma''' =$$

if $e'_1 = e'_3 \in (\text{const } c)$

$$K \text{ seq}(e'_1, e'_3)$$

o.w.

$$K(\text{if } e'_1 e'_2 e'_3)$$

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$\Gamma \text{ (assign } x \text{ } e) \gamma \vdash p \ k \sigma =$

$I \ e \ \text{Effect } p \ k \sigma \quad \text{if } p(x) = \text{Var}(x', op, s, lx') \text{ and ref} \in s$

$I \ e \ \text{Value } p \ k_1 \sigma \quad \text{o.w.} \quad \text{ref} \in s$

$$k_1 \ e' \ \sigma_1 = k \ \text{seq}(\text{assign } x' \ e'), (\text{const } c) \ \sigma_2$$

$$\sigma_2 = \sigma_1 [lx' \mapsto \text{Assign3} \cup \sigma_1(lx')]$$

$$c = \text{true if } \gamma = \text{Test} \quad \text{o.w.} \quad c = \text{void}$$

$\Gamma \text{ (primref } p) \gamma \vdash p \ k \sigma =$

$$\text{if } \gamma = \text{Test}, \ k \ (\text{const true}) \ \sigma$$

$$\gamma = \text{Effect}, \ k \ (\text{const void}) \ \sigma$$

$$\gamma = \text{Value}, \ k \ (\text{primref } p) \ \sigma$$

$$\gamma = \text{App}(op, \gamma_1, L\gamma), \ \text{fold } (\text{primref } p) \ \gamma \ p \ k \ \sigma$$

$\text{fold } (\text{primref } p) \ \text{App}(op, \gamma_1, L\gamma) \ p \ k \ \sigma = \text{visit}(op, \text{value}, k_1, \sigma)$

$$k_1 \ e' \ \sigma_1 = k \ (\text{primref } p) \ \sigma_1 \quad (\text{o.w.})$$

$$k \ (\text{const } c) \ \sigma_2 \quad \text{if } \text{result}(e') = (\text{const } c) \text{ and}$$

$$\text{where } \sigma_2 = \sigma_1 [L\gamma \mapsto \text{inlined3} \cup \sigma_1(L\gamma)] \ p(c) = c'$$

$\Gamma \text{ (call } e_1, e_2) \gamma \vdash p \ k \ \sigma =$

$$I \ e_1 \ \gamma_1 \ p \ k_1 \ \sigma_1$$

$$\text{where } op = \text{Opnd}(e_2, p, le_2) \quad le_2 \text{ fresh}$$

$$\gamma_1 = \text{App}(op, \gamma, le_1) \quad le_1 \text{ fresh}$$

$$\sigma_1 = \sigma [le_2 \mapsto \text{unvisited}, le_1 \mapsto \emptyset]$$

$$\begin{cases} \text{visit(Opnd}(e, p, le), \gamma, k, \sigma) \\ = I \ e \ \gamma \ p \ k \ \sigma \text{ if } \sigma(le) = \text{unvisit} \\ \text{where } k_1 = de' \sigma_1, k \ e' \ \sigma_1 [le \mapsto e'] \\ k \ e' \ \sigma \text{ where } \sigma(le) = e' \end{cases}$$

$$k_1 \ e'_1 \ \sigma_2 = \text{if inlined } \in \sigma_2(le_1), \ k \ e'_1 \ \sigma_2$$

$$\text{visit}(op, \text{value}, k_2, \sigma_2)$$

$$\text{where } k_2 \ e'_2 \ \sigma_3 = k \ (\text{call } e'_1 \ e'_2) \ \sigma_3$$

9-3/

$I (\lambda x. e) \gamma p k \sigma =$

$i + \gamma = \text{Test}, \quad k (\text{const true}) \sigma$

$\text{if } \gamma = \text{Effect}, \quad k (\text{const void}) \sigma$

$\text{if } \gamma = \text{App}(op, \gamma_1, \gamma_2), \quad \text{fold } (\lambda x. e) \gamma p k \sigma$

$\text{if } \gamma = \text{Value}, \quad I e \text{ Value } p, k, \sigma.$

$$x = \text{Var}(x, \text{null}, s, lx)$$

$$x' = \text{Var}(x', \text{null}, \sigma(lx), lx') \quad x', lx' \text{ fresh}$$

$$p_1 = p[x \mapsto x']$$

$$\sigma_1 = \sigma[lx' \mapsto \emptyset]$$

$$k_1 e' \sigma_2 = k (\lambda x'. e') \sigma_2$$

$\text{fold } (\lambda x. e) \text{ App}(op, \gamma_1, \gamma_2) p k \sigma =$

$I e \gamma_1 p_1 k_1 \sigma_1$

where $x = \text{Var}(x, \text{null}, s, lx)$

$$x' = \text{Var}(x', op, \sigma(lx), lx') \quad x', lx' \text{ fresh}$$

$$p_1 = p[x \mapsto x']$$

$$\sigma_1 = \sigma[lx' \mapsto \emptyset]$$

$$k_1 e' \sigma_2 = \begin{cases} \text{visit } (op, \text{Effect}, k_2, \sigma_2) & \text{if ref } \notin \sigma_2(lx') \text{ and assign } \in \sigma_2(lx') \\ \text{visit } (op, \text{Effect}, k_3, \sigma_2) & " \\ \text{visit } (op, \text{Value}, k_3, \sigma_2) & \text{assign } \in \sigma_2(lx') \end{cases}$$

$$k_2 e' \sigma_3 = k \text{ seg}(e'_1, e') \sigma_3 [l\gamma \mapsto \text{elim3} \cup \sigma_3(l\gamma)]$$

$$k_3 e' \sigma_3 = k (\text{call } (\lambda x'. e') e'_1) \sigma_3$$

Sketch

$I (\text{ref } x)$

$$p(x) = \text{Var}(\dots, op, \text{visit } (op, \dots))$$

