- A computer system can be abstractly represented by a pair of sets (Σ , Π), where
 - $\Sigma = \{ All possible allocation states of all system resources \}$
 - $\Pi = \{\text{Threads}\}\$
- Threads behave like functions, mapping one system state to another as they execute
- We say that a thread is blocked if it is in a system state from which it cannot run
- We say that a thread is deadlocked if a thread is blocked in the current system state, and in all future states the system can ever reach

- There are 4 necessary conditions for a deadlock to occur
 - The existence of mutually exclusive resources in a system (the mutex condition)
 - Such resources are broadly characterized as either serially reusable, or consumable
 - A hold-and-wait condition in the system
 - A no-preemption condition in the system
 - A circular wait condition in the system

- There are 4 areas of deadlock study that have been researched extensively:
 - Deadlock prevention
 - Deadlock avoidance
 - Deadlock detection
 - Deadlock recovery as an extension of detection

- Prevention involves denying a necessary condition and is always "expensive"
- Avoidance employs policy decisions which may hold-back resources to maintain "safe states"
- Detection is generally achieved by the construction and reduction of Resource Allocation Graphs (RAGs ... bipartite graphs with thread and resource nodes)
- Recovery generally involves thread termination and is often based on ad-hoc policies at a given site



- Prevention may be achieved by denying any one of the necessary conditions:
 - Exclusively accessed resources
 - since things as basic as a memory location can fall in this category, we have to live with this condition
 - Hold and wait condition
 - a-priori resource allocation (the policy employed can lead to its own deadlock)
 - resource under-utilization (RU)

- Prevention (continued)
 - No preemption
 - lost work
 - indefinite postponement (IP)
 - Circular wait
 - appropriate resource ordering
 - RU
 - changes may go all the way back to application sources

- Avoidance
 - Safe and unsafe states
 - no single resource allocation can lead directly to deadlock from a safe state
 - consider the following system of 3 threads and 10 tape drives:

THREAD	CURRENT	MAX	BALANCE
А	2	4	2
В	3	6	3
С	3	8	5

If A asks for 1 drive should the request be granted ? If B asks for 1 drive should the request be granted ?

- Detection
 - RAG reduction ... bipartite, M res, N threads
 - Cycle is necessary condition for deadlock in all cases, but is sufficient in AND model reusable only systems









- Complexity of reduction:
 - For GENERAL graphs:
 - O(MN!)
 - For REUSABLE ONLY graphs:
 - O(MN)